Math 107
Fall 2017
Lecture 10

find $x$, then the measure of marked angles:


$$
3(10)+45
$$

$$
=30+45
$$

$$
7(10)+5
$$

$$
\begin{aligned}
& =70+5 \\
& =750^{\circ}
\end{aligned}
$$

Hint: They are vertical angles, therefore, they must be equal.

$$
\begin{aligned}
7 x+5 & =3 x+45 \\
7 x-3 x & =45-5 \\
4 x & =40 \\
x & =\frac{40}{4} \quad x=10
\end{aligned}
$$

find $x$, then find the measure of marked
angles
 Hint: Adjacent angles are supplementary, therefore their sum is $180^{\circ}$

$$
17 x=180-10
$$

$$
17 x=170
$$

$$
\left\{\begin{array}{l}
x=\frac{170}{17} \quad x=10 \\
7(10)+3=\left\{\begin{array}{l}
73^{\circ} \\
10(10)+7=107^{\circ}
\end{array}\right. \\
\underbrace{73^{\circ} \dot{1} 107^{\circ}}
\end{array}\right.
$$

Angles $A$ and $B$ are complementary.
Angle $A$ is two more than 3 times angle $B$.

$$
\begin{aligned}
& \text { find both angles. } \\
& A \rightarrow 3 x+2 \\
& 3 x+2+x=90 \\
& B \rightarrow x \\
& B \rightarrow 22^{\circ} \\
& \begin{array}{r}
4 x+2=90 \\
4 x=90-2 \\
4 x=88
\end{array} \\
& \begin{array}{r}
4 x+2=90 \\
4 x=90-2 \\
4 x=88
\end{array} \\
& A \rightarrow 3(22)+2 \\
& A \rightarrow 68^{\circ} \\
& A+B=90^{\circ} \\
& \sigma \quad b \\
& x=\frac{88}{4} \quad x=22
\end{aligned}
$$

Angles $A$ and $B$ are supplementary angles.
Angle $A$ is 3 times angle $B$.
find both angles.

$$
A+B=180^{\circ}
$$

$$
\begin{aligned}
& B \rightarrow x \rightarrow 45^{\circ} \\
& A \rightarrow 3 x \rightarrow 3(45)=135^{\circ}
\end{aligned} \begin{aligned}
& 3 x+x=180 \\
& 4 x=180 \\
& 45^{\circ} \dot{1} 135^{\circ}
\end{aligned}
$$

Find an angle such that
its supplement is $39^{\circ}$ more than twice its

$$
\begin{array}{l|l|l}
\text { Angle } & \text { Complement } & \text { Supplement } \\
\hline x & 90-x & 180-x \\
\text { Supplement }=2 \text { Complement }+39 \\
180-x=2(90-x)+39 \\
180-x=180-2 x+39 \\
-x+2 x=180+39-180
\end{array} \quad \begin{aligned}
& \text { Complement. }
\end{aligned}
$$

find an angle such that the sum of its complement and its supplement is $160^{\circ}$

| Angle | Comp. | Suppl. |
| :---: | :---: | :---: |
| $x$ | $90-x$ | $180-x$ |

Compl. + Suppl $=160$
$90-x+180-x=160$
(270) $-2 x=160$

$$
-2 x=160-270-
$$

$$
\left\{\begin{array}{c}
-2 x=-110 \\
x=\frac{-110}{-2} \\
x=55 \\
55^{\circ}
\end{array}\right.
$$

find an angle whose supplement is $38^{\circ}$ less than 3 times its complement.

$$
\begin{array}{l|l|l}
\text { Angle } & \text { Comp. } & \text { Suppl. } \\
\hline x & 90-x & \text { r80-x } \\
\text { Suppl. }=3 \cdot \text { Comp. }-38 \\
180-x=3 \cdot(90-x)-38 \\
180-x=270-3 x-38 \\
-x+3 x=270-38-180
\end{array} \quad\left[\begin{array}{c}
2 x=52 \\
x=\frac{52}{2} \\
x=26
\end{array}\right.
$$

I have 3 Dimes and 7 Quarters.
How much money do I have?

$$
3(10 \$)+7(25 \$)=205 \$=\$ 2.05
$$

Lisa has $\$ 2.05$ in dimes $\frac{1}{1}$ Quarters c.nly. \# of Quarters is 1 more than twice \# of dimes. How many of each does she have?

Dimes $\rightarrow x$

$$
\text { Quarters }>2 x+1
$$

$$
\begin{aligned}
10 x+25(2 x+1) & =205 \\
10 x+50 x+25 & =205 \\
60 x+25 & =205
\end{aligned}
$$

$$
60 x=205-25
$$

$$
\begin{aligned}
60 x & =180 \\
x & =\frac{180}{60} \quad x=3
\end{aligned}
$$

3 Dimes 2(3)+1 Quarters


